

Cambridge IGCSE®

CANDIDATE NAME										
CENTRE NUMBER								NDIDATE IMBER		

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ADDITIONAL MATHEMATICS

0606/01

2 hours

Paper 1

For examination from 2020

SPECIMEN PAPER

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Blank pages are indicated.

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Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$
 where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series

$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$$

Geometric series

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \quad (|r| < 1)$$

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$\Delta = \frac{1}{2} bc \sin A$$

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1 DO NOT USE A CALCULATOR IN THIS QUESTION.

The polynomial $p(x) = 2x^3 - 3x^2 + qx + 56$ has a factor x - 2.

(a) Show that q = -30. [1]

(b) Factorise p(x) completely and hence state all the solutions of p(x) = 0. [4]

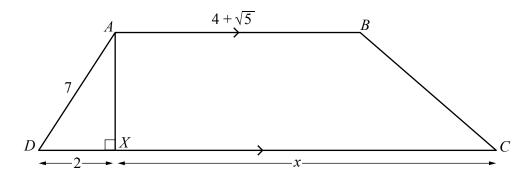
- 2 Variables x and y are related by the equation $y = x\sqrt{x}$.
 - (a) Find $\frac{dy}{dx}$. [2]

(b) Hence find the approximate change in x when y increases from 8 by the small amount 0.015. [3]

3 (a) Express $12x^2 - 6x + 5$ in the form $p(x-q)^2 + r$, where p, q and r are constants to be found. [3]

(b) Hence find the greatest value of $(12x^2 - 6x + 5)^{-1}$ and state the value of x at which this occurs.

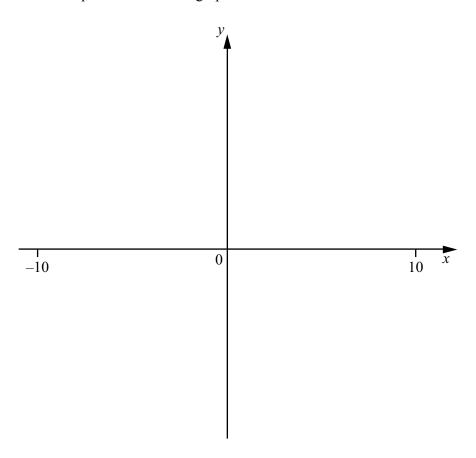
4 DO NOT USE A CALCULATOR IN THIS QUESTION.



The diagram shows a trapezium ABCD in which AD = 7 cm and $AB = (4 + \sqrt{5})$ cm. AX is perpendicular to DC with DX = 2 cm and XC = x cm.

Given that the area of trapezium ABCD is $15(\sqrt{5} + 2)$ cm², obtain an expression for x in the form $a + b\sqrt{5}$, where a and b are integers. [6]

5 (a) On the axes below, sketch the graph of y = |2x + 5| and the graph of y = |2 - x|, stating the coordinates of the points where each graph meets the coordinate axes. [4]



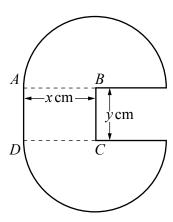
(b) Solve
$$|2x+5| \le |2-x|$$
. [3]

6 Find the equation of the normal to the curve $y = \frac{2x-1}{\sqrt{x^2+5}}$ at the point where x = 2.

Give your answer in the form ax + by = c, where a, b and c are integers.

[8]

7



The diagram shows a badge, made of thin sheet metal, consisting of two semi-circular pieces, centres B and C, each of radius x cm. They are attached to each other by a rectangular piece of thin sheet metal, ABCD, such that AB and CD are the radii of the semicircular pieces and AD = BC = y cm.

(a) Given that the area of the badge is $20 \,\mathrm{cm}^2$, show that the perimeter, $P \,\mathrm{cm}$, of the badge is given by

$$P = 2x + \frac{40}{x}.\tag{4}$$

(b) Given that x can vary, find the minimum value of P, justifying that this value is a minimum. [5]

8 (a) Giving your answer in its simplest form, find the exact value of

(i)
$$\int_{0.2}^{1} e^{5x-1} dx$$
, [4]

(ii)
$$\int_{1}^{2} \left(x + \frac{1}{x^2} \right)^2 dx$$
. [5]

(b) Find
$$\int \sin \frac{x}{6} dx$$
. [2]

9 DO NOT USE A CALCULATOR IN THIS QUESTION.

In the expansion of $(1+2x)^n$, the coefficient of x^4 is ten times the coefficient of x^2 .

Find the value of the positive integer n.

[6]

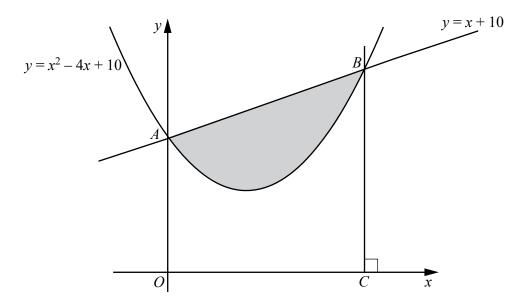
10	(a)	An arithmetic	progression	has a first	term of 5 a	and a common	difference of -3 .
- 0	\ •• <i>/</i>	I III WIITIIIIO	progression	mas a misse	COLLIE OF C	alla a collillion	difference of 5.

Find the number of terms such that the sum to n terms is first less than -200. [4]

- **(b)** A geometric progression is such that its 3rd term is equal to $\frac{81}{64}$ and its 5th term is equal to $\frac{729}{1024}$.
 - (i) Find the first term of this progression and the positive common ratio of this progression. [5]

(ii) Hence find the sum to infinity of this progression.

11



The graph of $y = x^2 - 4x + 10$ cuts the y-axis at point A. The graphs of $y = x^2 - 4x + 10$ and y = x + 10 intersect one another at the points A and B. The line BC is perpendicular to the x-axis. Calculate the area of the shaded region enclosed by the curve and the line AB. [8]

Continuation of working space for question 11.

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